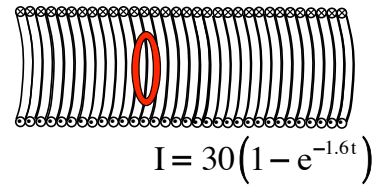


### Problem 31.14

With Faraday's Law problems (i.e., Induction problems), you always want to determine the magnetic field, then the magnetic flux, then take the derivative. The solenoid generates a magnetic field of:

$$\begin{aligned} B_{\text{solenoid}} &= (\mu_o nI) \\ &= (4\pi \times 10^{-7} \text{ T}\cdot\text{m/A})(400 \text{ turns/m})[30(1 - e^{-1.6t}) \text{ A}] \\ &= 1.5 \times 10^{-2} (1 - e^{-1.6t}) \text{ T} \end{aligned}$$

$$n_{\text{solenoid}} = 400 \text{ turns/meter}$$
$$N_{\text{coil}} = 250 \text{ turns}, \quad R_{\text{coil}} = .06 \text{ m}$$

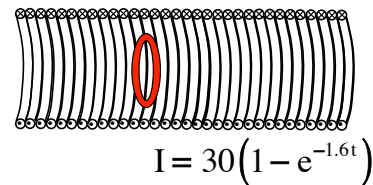


1.)

The magnetic flux through the coil is a function of the cross-sectional area of the coil, so:

$$\begin{aligned} \Phi_B &= \vec{B} \cdot \vec{A} \\ &= [\mu_o nI](\pi R_{\text{coil}}^2) \\ &= [1.5 \times 10^{-2} (1 - e^{-1.6t})](\pi (.06 \text{ m})^2) \\ &= 1.7 \times 10^{-4} (1 - e^{-1.6t}) \text{ Webers} \end{aligned}$$

$$n_{\text{solenoid}} = 400 \text{ turns/meter}$$
$$N_{\text{coil}} = 250 \text{ turns}, \quad R_{\text{coil}} = .06 \text{ m}$$



And the EMF is:

$$\begin{aligned} \mathcal{E}_{\text{induced}} &= -N_{\text{coil}} \frac{d\Phi_B}{dt} \\ &= -(250) \left[ \frac{d(1.7 \times 10^{-4} (1 - e^{-1.6t}) \text{ Webers})}{dt} \right] \\ &= -(250)(1.7 \times 10^{-4})(-1.6)e^{1.6t} \text{ V} \\ &= 6.8 \times 10^{-2} e^{1.6t} \text{ V} \end{aligned}$$

2.)